

CSCI235 Database Systems

Beyond BCNF

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Beyond BCNF

Outline

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Data explosion problem

A relational schema

`EMP(employee-number, programming-language, operating-system)`

has no valid functional dependencies

A relational table `EMPLOYEE` over a relational schema `EMP` contains information about the programming languages and operating systems known by employees

employee-number	programming-language	operating-system	EMPLOYEE
200	Python	Linux	
200	Java	Linux	
200	Scala	Linux	
200	Python	Windows 10	
200	Java	Windows 10	
200	Scala	Windows 10	

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Data explosion problem

employee-number	programming-language	operating-system	EMPLOYEE
200	Python	Linux	
200	Java	Linux	
200	Scala	Linux	
200	Python	Windows	
200	Java	Windows	
200	Scala	Windows	
200	Fortran	Linux	
200	Fortran	Windows	
200	Python	Unix	
200	Java	Unix	
200	Scala	Unix	
200	Fortran	Unix	

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Data explosion problem

employee-number	programming-language	operating-system	EMPLOYEE
200	Python	Linux	
200	Java	Linux	
200	Scala	Linux	
200	Python	Windows	
200	Java	Windows	
200	Scala	Windows	
200	Fortran	Linux	
200	Fortran	Windows	
200	Python	Unix	
200	Java	Unix	
200	Scala	Unix	
200	Fortran	Unix	

Normal form ?

No valid functional dependencies means that does not exists a functional dependence such that its left hand side is not a superkey

It means that no functional dependencies violate **BCNF**

BCNF but ... still a lot of redundancies !

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Multivalued dependency

Let $R = (A_1, \dots, A_n)$ be a relational schema and let X, Y, Z be nonempty subsets of R

We say that a multivalued dependency $X \twoheadrightarrow Y | Z$ is valid in relational schema R if ...

... for any relational table r created over a relational schema R , if for any two rows v and w in r such that $v[X] = w[X]$ there exist a row t in r such that ...

... $v[XY] = t[XY]$ and $w[XZ] = t[XZ]$

Other notation

X	Y	
X		Z

X	Y	Z

Multivalued dependency

It means that if a row $x \ y \ \square$ is in a relational table and a row $x \ \square \ z$ is in the same table then a row $x \ y \ z$ must be in the same relational table

Multivalued dependency

Examples

employee-number $\twoheadrightarrow$ programming-language | operating-system

employee-number	programming-language		Multivalued dependency
employee-number		operating-system	
employee-number	programming-language	operating-system	

A person owns many cars and has many skills

first-name, last-name $\twoheadrightarrow$ registration-number | skill

A students has many friends and many hobbies

student-number $\twoheadrightarrow$ first-name, last-name | hobby

<pre>CREATE VIEW XY AS (SELECT X,Y FROM R); CREATE VIEW XZ AS (SELECT X,Z FROM R); SELECT XY.X, XY.Y, XZ.Z FROM XY JOIN XZ ON XY.X = XZ.X</pre>	Multivalued dependency
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The result of **SELECT** is always equal to **R**

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4NF

A relational schema R is in the **Fourth Normal Form (4NF)** if for every nontrivial multivalued dependency $X \twoheadrightarrow Y|Z$ a set of attributes X is a superkey in a relational schema R

Alternative definition:

A relational schema R is in **4NF** if no nontrivial multivalued dependencies are valid in a relational schema R

A multivalued dependency

$\text{employee-number} \twoheadrightarrow \text{programming-language} | \text{operating-system}$

is valid in a relational schema

$\text{EMP}(\text{employee-number}, \text{programming-language}, \text{operating-system})$

A relational schema EMP is **NOT** in **4NF** because a nontrivial multivalued dependency is valid in EMP

4NF

Decomposition into 4NF ?

EPGM(employee-number, programming-language),
EOPS(employee-number, operating-system)

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Join dependency

Let $R = (A_1, \dots, A_n)$ be a relational schema and let $X, Y_1, \dots, Y_n$ be nonempty subsets of R

We say that join dependency $\bowtie(X, Y_1, \dots, Y_n)$ is valid in a relational schema R if ...

... for any relational table r with relational schema R , if for any n rows $v_1, \dots, v_n$ in r such that $v_1[X] = \dots = v_n[X]$ there exist a row t in r such that ...

... $v_1[XY_1] = t[XY_1]$ and ... and $v_n[XY_n] = t[XY_n]$

Other notation

X	Y1				
X		Y2			
X			Y3		
...	...	...	...		
X	...	...	...	YN	
X	Y1	Y2	Y3	...	YN

Multivalued dependency

Join dependency

Examples

⌋(employee-number, programming-language, operating-system, hobby)

employee-number	programming-language			Join dependency
employee-number		operating-system		
employee-number			hobby	
employee-number	programming-language	operating-system	hobby	

A person owns many cars and has many skills and has many employers

⌋((first-name, last-name), registration-number, skill, employer)

```
CREATE VIEW XY1 AS (SELECT X,Y1 FROM R);
CREATE VIEW XY2 AS (SELECT X,Y2 FROM R);
... ..
CREATE VIEW XYN AS (SELECT X,YN FROM R);
SELECT XY1.X, XY1.Y1, XY2.Y2, ... XYN.YN
FROM XY1 JOIN XY2 ON XY1.X = XY2.X JOIN ... JOIN XYN ON XY1.X = XYN.X
```

The result of **SELECT** is always equal to **R**

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5NF

A relational schema R is in the **Fifth Normal Form (5NF)** if for every nontrivial join dependency $\bowtie(X, Y_1, \dots, Y_n)$ a set of attributes X is a superkey in R

Alternative definition:

A relational schema R is in **5NF** if no nontrivial join dependencies are valid in schema R

A join dependency $\bowtie(\text{employee-number}, \text{programming-language}, \text{operating-system}, \text{hobby})$ is valid in a relational schema $\text{EMP}(\text{employee-number}, \text{programming-language}, \text{operating-system}, \text{hobby})$

A relational schema EMP is **NOT** in **5NF** because a nontrivial join dependency is valid in EMP

5NF

Decomposition into 5NF ?

EPGM(employee-number, programming-language),
EOPS(employee-number, operating-system),
EHOB(employee-number, hobby)

References

T. Connolly, C. Begg, Database Systems, A Practical Approach to Design, Implementation, and Management, Chapter 15.4 Fourth Normal Form (4NF), Chapter 15.5 Fifth Normal Form (5NF), Pearson Education Ltd, 2015